

CÁLCULO

$$0, 1, 2, 3, 5, 8, 13, \dots, n$$

M_n M_{n+1}

$$\lim_{n \rightarrow \infty} \frac{M_{n+1}}{M_n} = \frac{1 + \sqrt{5}}{2} \approx 1,618034 \dots \quad (1)$$

Dividir (1)

$$M_{n+1} = M_n + M_{n-1} \quad (2)$$

$$\frac{M_{n+1}}{M_n} = 1 + \frac{M_{n-1}}{M_n} \quad (3)$$

$$\lim_{n \rightarrow \infty} \frac{M_{n+1}}{M_n} = L \quad (4)$$

$$\frac{1}{L} = \lim_{n \rightarrow \infty} \frac{M_{n-1}}{M_n} \quad (5)$$

$$\lim_{n \rightarrow \infty} \frac{M_{n+1}}{M_n} = 1 + \frac{1}{L} \quad (6)$$

$$L = 1 + \frac{1}{L} \quad (7)$$

$$L^2 = L + 1 \quad (8)$$

$$L = \frac{1 + \sqrt{5}}{2} = 7$$

$$X^2 - X - 1 = 0$$

$$X = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

2º GRADO

$$a=1 \quad b=-1 \quad c=-1$$

$$L^2 - L - 1 = 0 \quad (9)$$

$$L = \frac{1 \pm \sqrt{1^2 + 4}}{2}$$

$$L = \frac{1 + \sqrt{5}}{2}$$

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GEOMETRIA



$$\alpha = \frac{1-x}{x}$$

$$= 1,618034 \dots$$

$$x^2 = -x + 1 \quad (2)$$

$$x^2 + x - 1 = 0 \quad (3)$$

$$x = \frac{-1 \pm \sqrt{5}}{2}$$

$$x = \frac{-1 + \sqrt{5}}{2}$$

$$\frac{1}{x} = \frac{2}{-1 + \sqrt{5}}$$

$$= \alpha$$

$$\frac{1}{x} = \frac{2(1 + \sqrt{5})}{(-1 + \sqrt{5})(1 + \sqrt{5})}$$

$$= \frac{2 + 2\sqrt{5}}{-1 - \sqrt{5} + 1 + 5}$$

$$= \frac{2 + 2\sqrt{5}}{4}$$

$$= \frac{1 + \sqrt{5}}{2} = 4$$

$$\alpha = 1,618034$$