

<https://youtu.be/MjhAIQz9UZc>

## 3 – A DERIVADA – CÁLCULO DIFERENCIAL

17 EQUAÇÕES QUE MUDARAM O MUNDO – OUTSPOKEN MARKET NA PRÁTICA – LEANDRO GUERRA

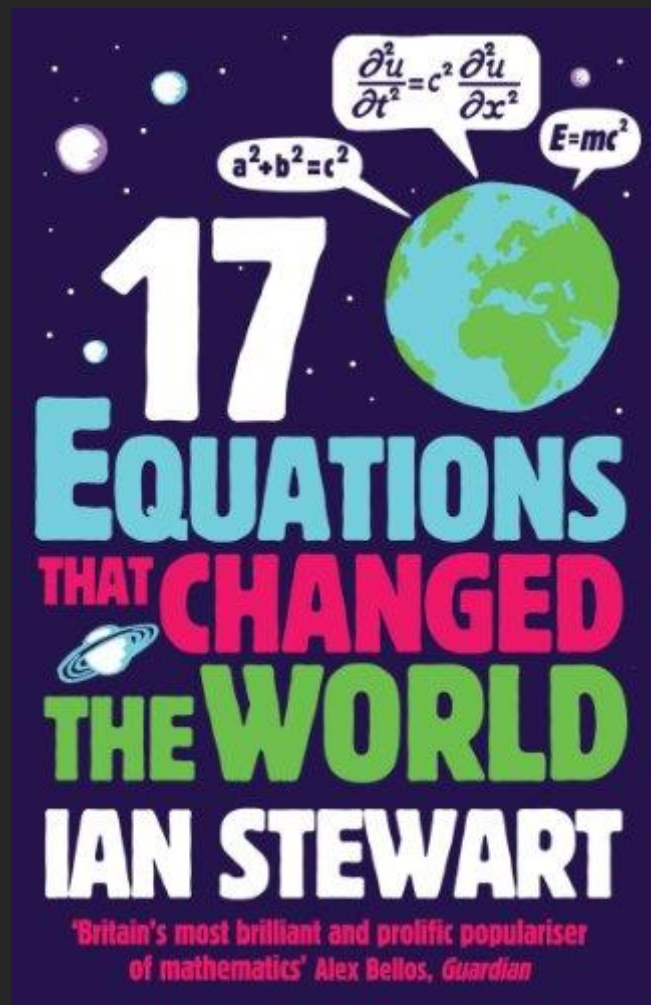


$$\frac{dy}{dx} = \lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$$

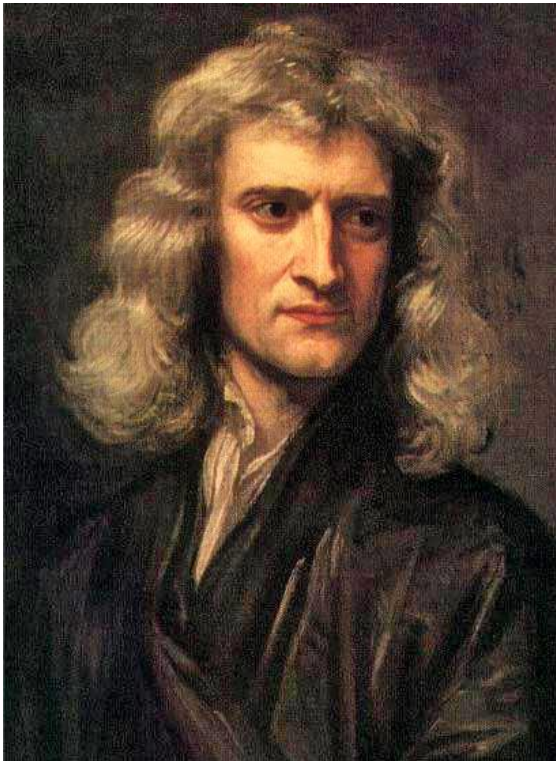
$$m = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

## 17 Equations That Changed the World by Ian Stewart

1. **Pythagoras's Theorem**  $a^2 + b^2 = c^2$  Pythagoras, 530 BC
2. **Logarithms**  $\log xy = \log x + \log y$  John Napier, 1610
3. **Calculus**  $\frac{df}{dt} = \lim_{h \rightarrow 0} \frac{f(t+h) - f(t)}{h}$  Newton, 1668
4. **Law of Gravity**  $F = G \frac{m_1 m_2}{r^2}$  Newton, 1687
5. **The Square Root of Minus One**  $i^2 = -1$  Euler, 1750
6. **Euler's Formula for Polyhedra**  $V - E + F = 2$  Euler, 1751
7. **Normal Distribution**  $\Phi(x) = \frac{1}{\sqrt{2\pi\rho}} e^{-\frac{(x-\mu)^2}{2\rho}}$  C.F. Gauss, 1810
8. **Wave Equation**  $\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$  J. d'Alembert, 1746
9. **Fourier Transform**  $f(\omega) = \int_{-\infty}^{\infty} f(x) e^{-2\pi i x \omega} dx$  J. Fourier, 1822
10. **Navier-Stokes Equation**  $\rho \left( \frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = -\nabla p + \nabla \cdot \mathbf{T} + \mathbf{f}$  C. Navier, G. Stokes, 1845
11. **Maxwell's Equations**  $\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$   $\nabla \cdot \mathbf{H} = 0$   $\nabla \times \mathbf{E} = -\frac{1}{c} \frac{\partial \mathbf{H}}{\partial t}$   $\nabla \times \mathbf{H} = \frac{1}{c} \frac{\partial \mathbf{E}}{\partial t}$  J.C. Maxwell, 1865
12. **Second Law of Thermodynamics**  $dS \geq 0$  L. Boltzmann, 1874
13. **Relativity**  $E = mc^2$  Einstein, 1905
14. **Schrodinger's Equation**  $i\hbar \frac{\partial}{\partial t} \Psi = H\Psi$  E. Schrodinger, 1927
15. **Information Theory**  $H = -\sum p(x) \log p(x)$  C. Shannon, 1949
16. **Chaos Theory**  $x_{i+1} = kx_i(1 - x_i)$  Robert May, 1975
17. **Black-Scholes Equation**  $\frac{1}{2}\sigma^2 S^2 \frac{\partial^2 V}{\partial S^2} + rS \frac{\partial V}{\partial S} + \frac{\partial V}{\partial t} - rV = 0$  F. Black, M. Scholes, 1990



# ISAAC NEWTON OU LEIBNIZ?

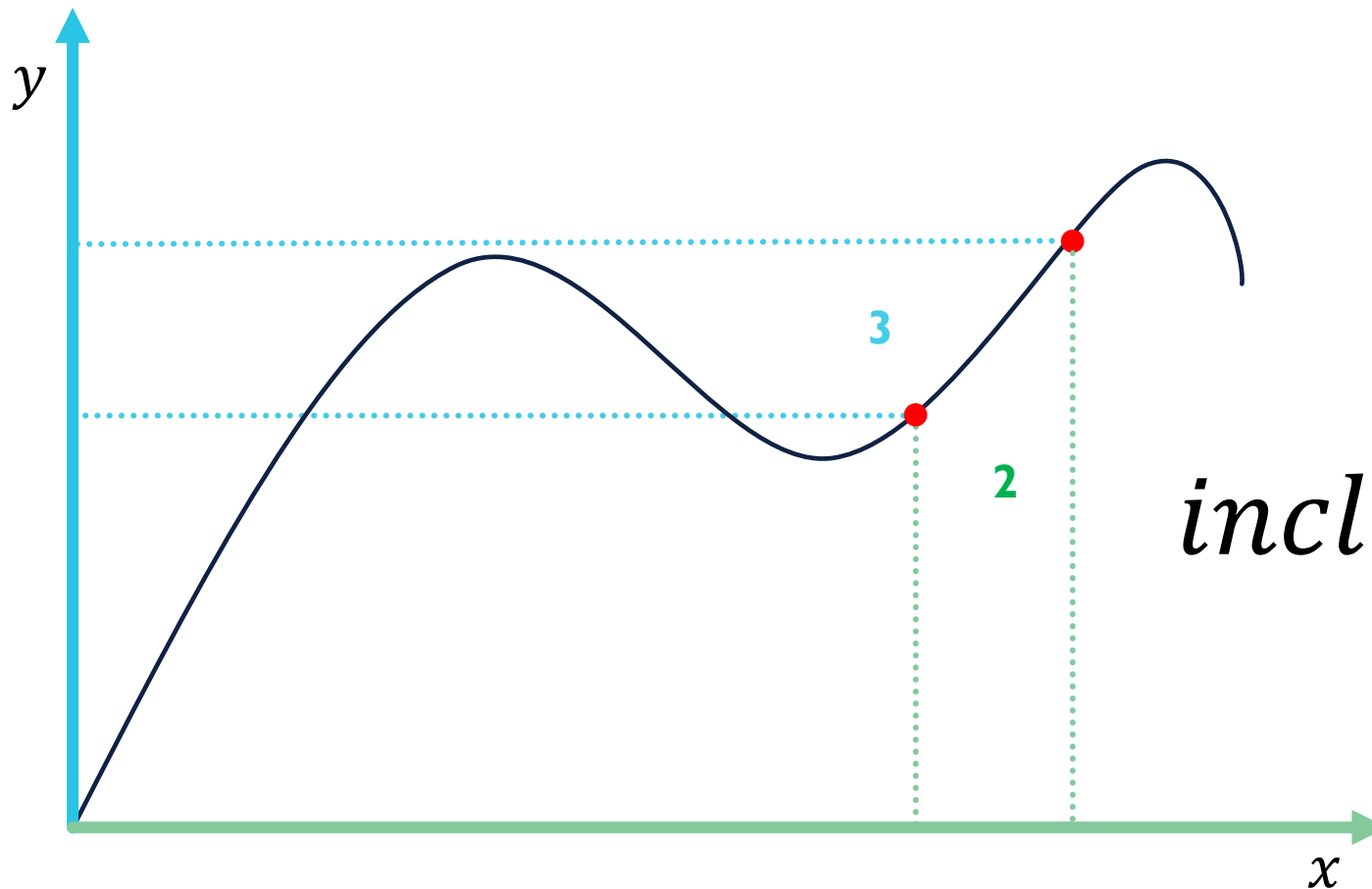


Isaac Newton  
(1642 -1726)



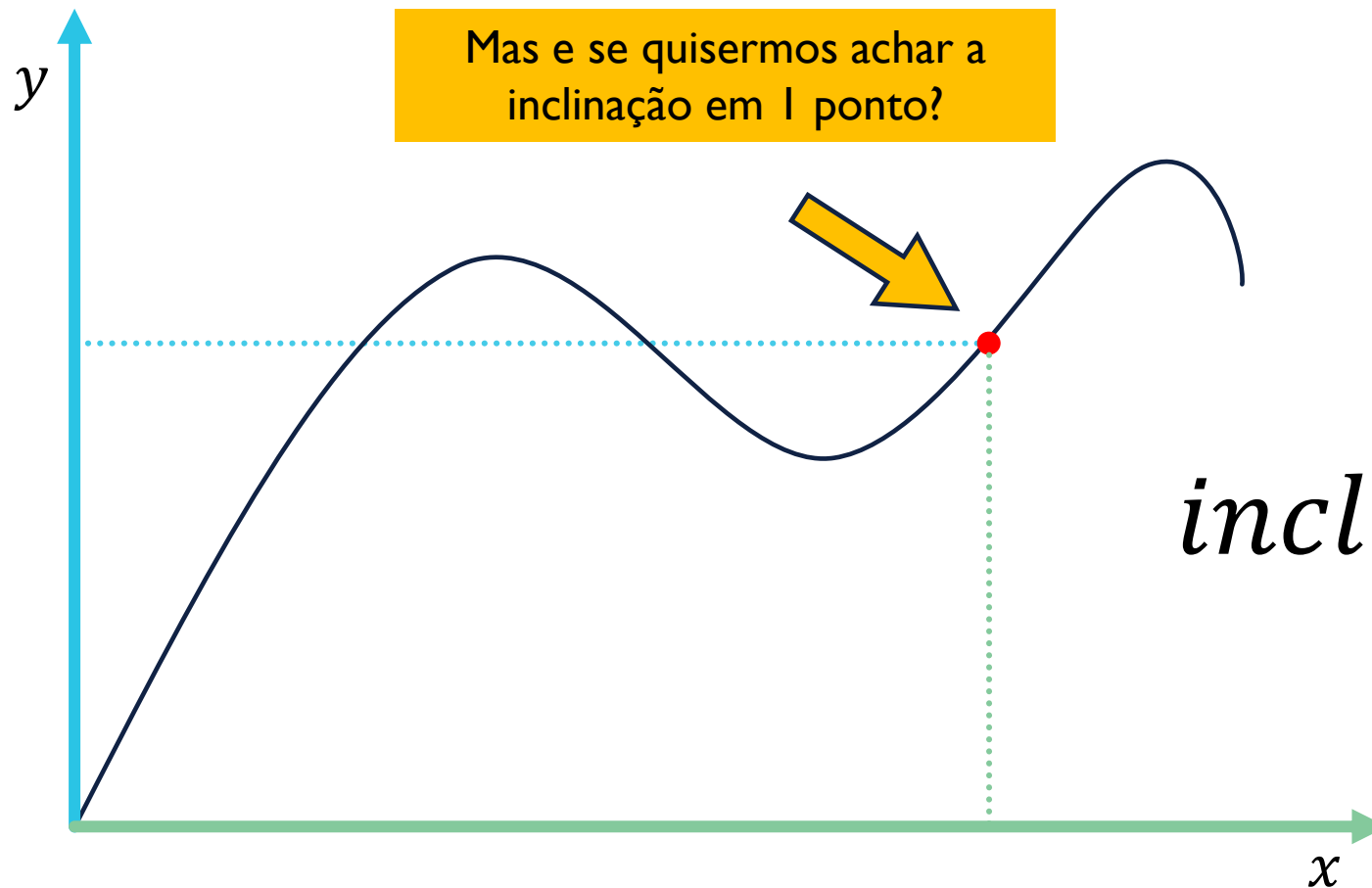
Gottfried Wilhelm Leibniz  
(1646 -1716)

# PENSE EM INCLINAÇÃO E TAXA DE VARIAÇÃO



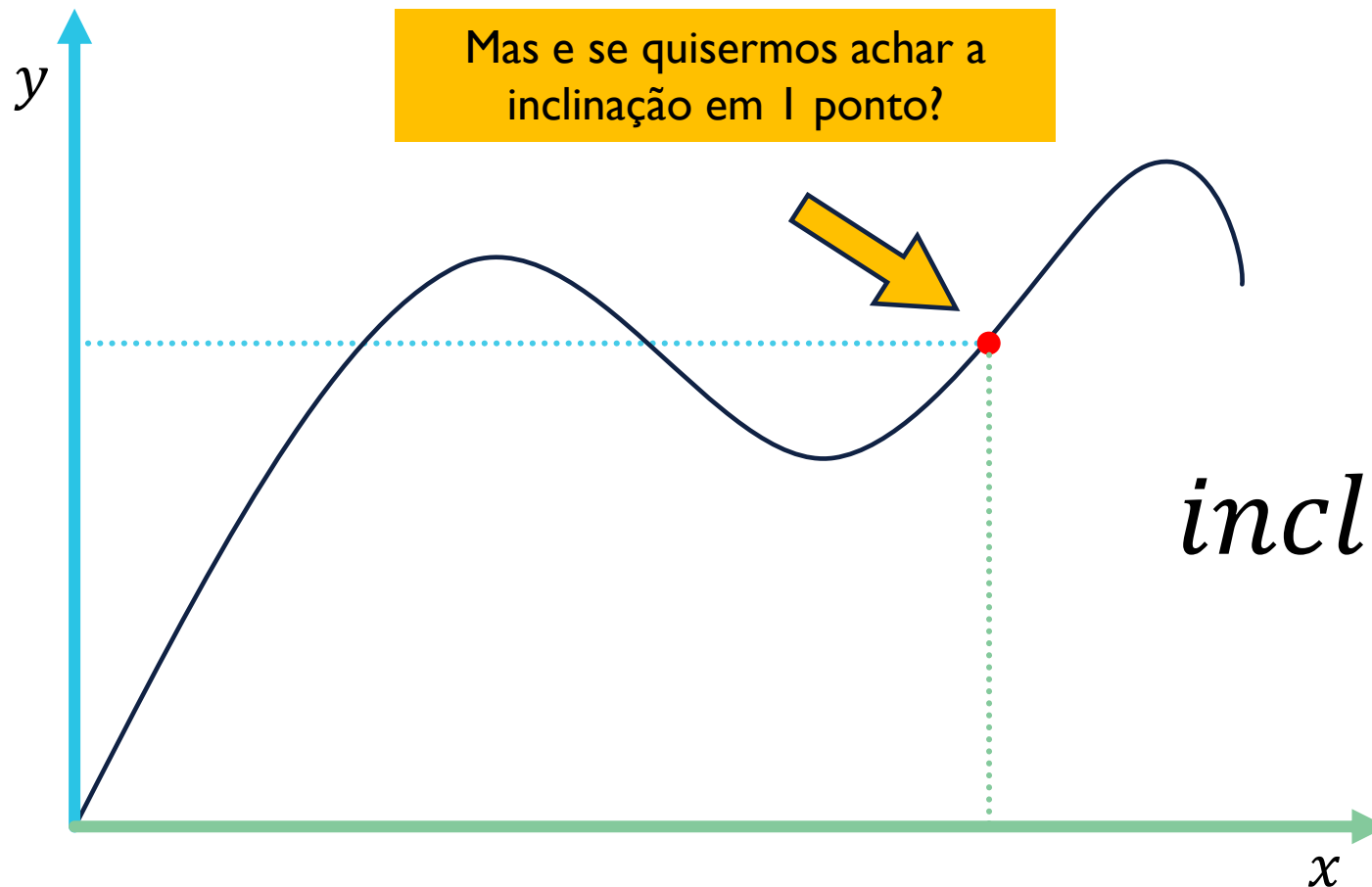
$$\textit{inclinação} = \frac{3}{2} = 1,5$$

# PENSE EM INCLINAÇÃO E TAXA DE VARIAÇÃO



$$\textit{inclinação} = \frac{0}{0} = ?$$

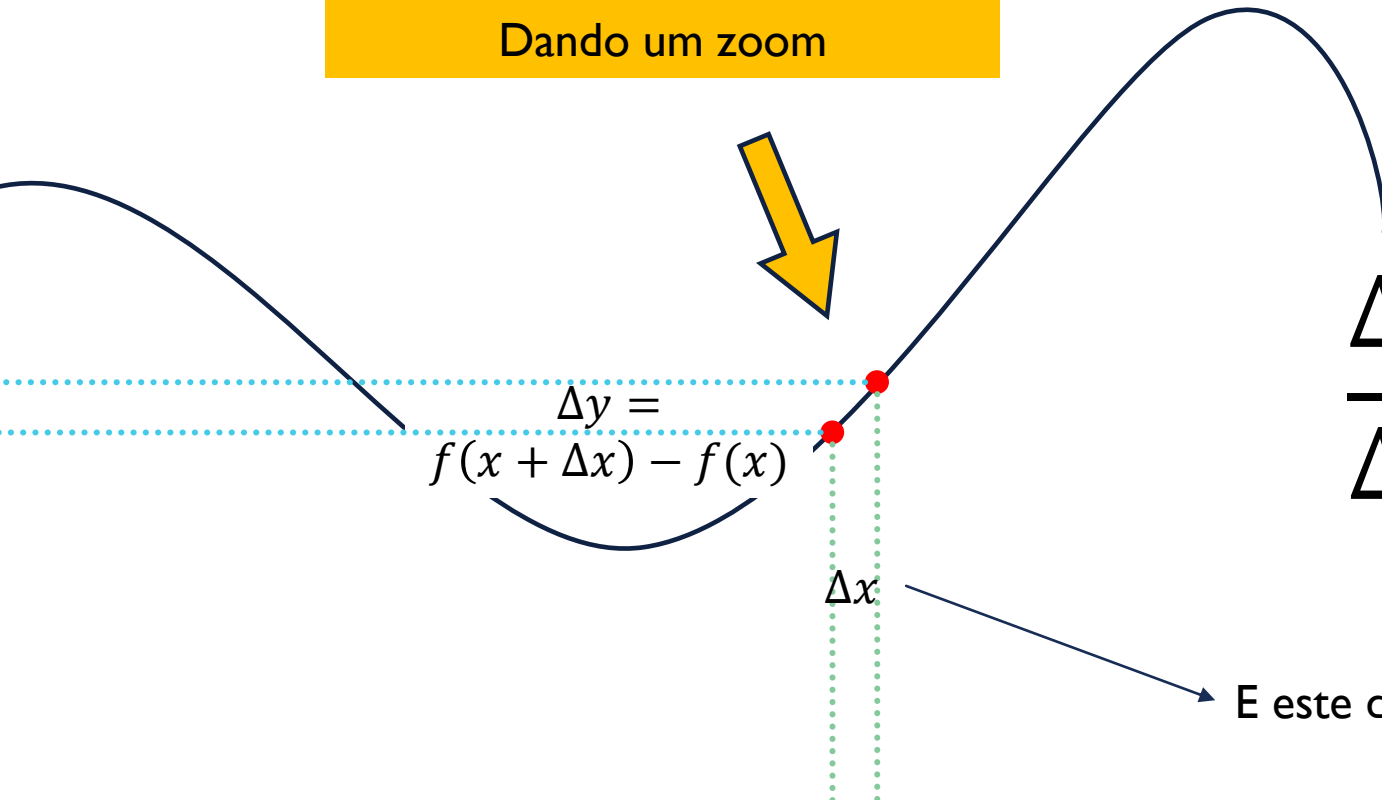
# PENSE EM INCLINAÇÃO E TAXA DE VARIAÇÃO



$$\textit{inclinação} = \frac{\Delta y}{\Delta x} = ?$$

# PENSE EM INCLINAÇÃO E TAXA DE VARIAÇÃO

Dando um zoom



$$\frac{\Delta y}{\Delta x} = \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

E este delta x tende a zero



## EXEMPLO CLÁSSICO

Dado  $f(x) = x^2$  qual  $f'(x) = x^2$ ?

$$\frac{\Delta y}{\Delta x} = f'(x) = \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

$$f'(x) = \frac{(x^2 + 2x \cdot \Delta x + \Delta x^2) - x^2}{\Delta x}$$

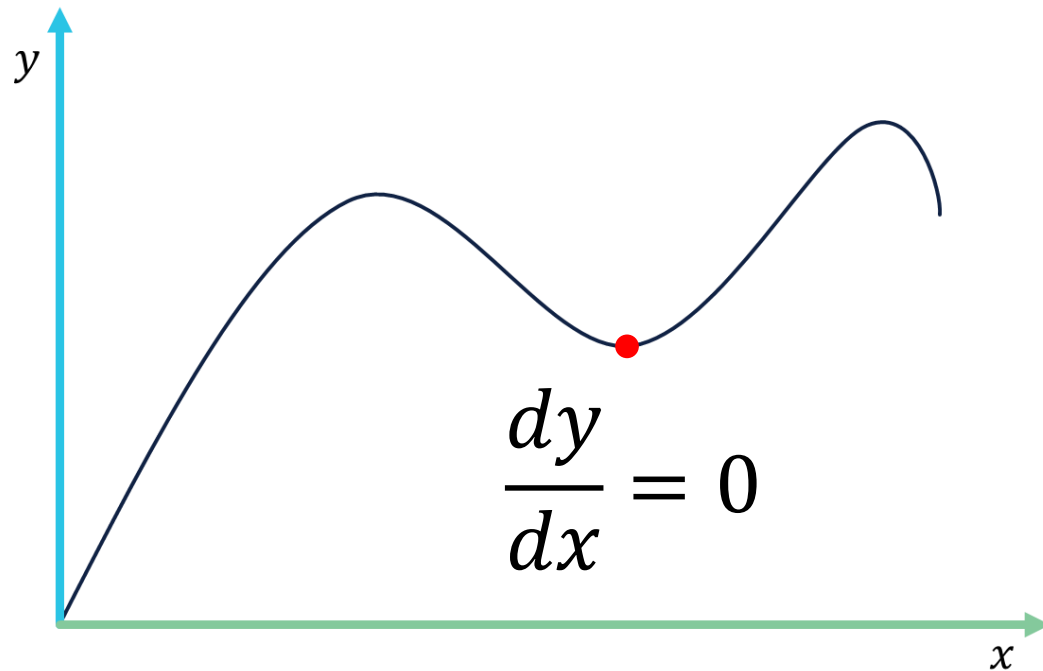
$$f'(x) = \frac{2x \cdot \Delta x + \Delta x^2}{\Delta x}$$

Como o delta x tende a zero

$$f'(x) = 2x \rightarrow \frac{dy}{dx}$$

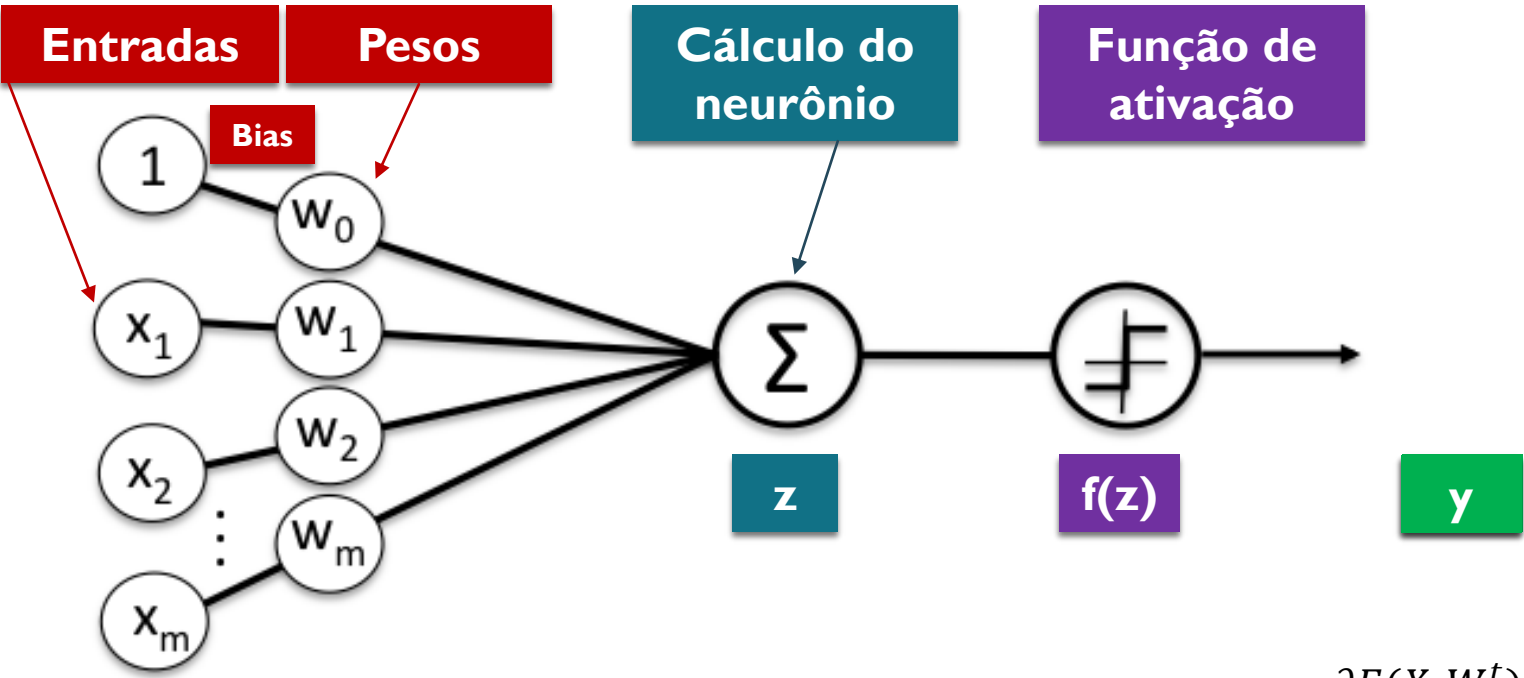
## E PARA O QUE ISSO SERVE?

Achar o ponto de mínimo ou máximo de uma função!



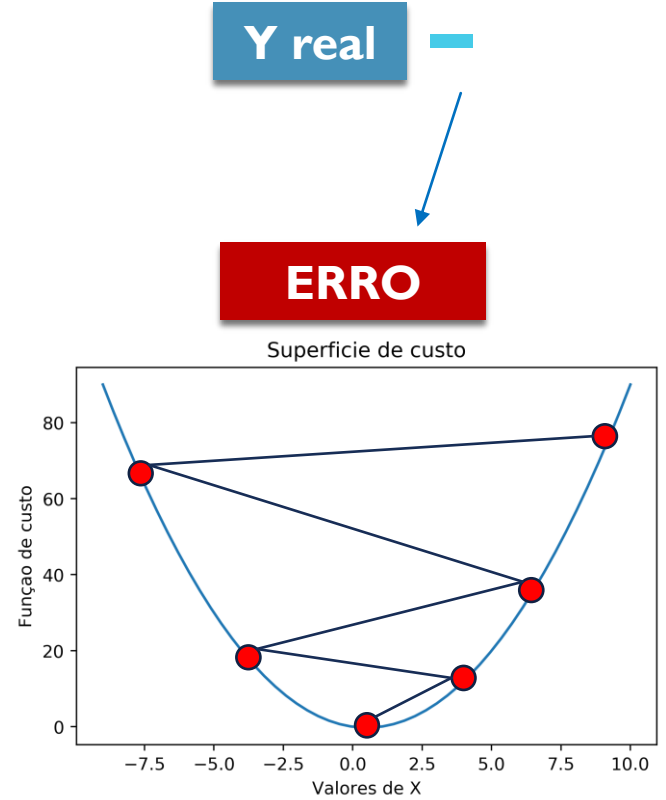
O ponto mínimo é onde a derivada é igual a zero!  
Não existe inclinação!

# TREINAMENTO DE MODELOS MATEMÁTICOS!



$$W^{t+1} = W^t - \alpha \frac{\partial E(X, W^t)}{\partial W}$$

**Derivada da Função de Erro**



# O MODELO DE BLACK-SCHOLES

$$\frac{1}{2} \sigma^2 S^2 \frac{\partial^2 V}{\partial S^2} + rS \frac{\partial V}{\partial S} + \frac{\partial V}{\partial t} - rV = 0$$

**Gamma**

**Delta**

**Theta**

$r =$  taxa livre de risco

$S =$  preço do ativo

$V =$  preço da opção

$\sigma =$  volatilidade implícita



# OBRIGADO E ATÉ A PRÓXIMA!

OUTSPOKEN MARKET

